## Problem 27

Suppose you walk 18.0 m straight west and then 25.0 m straight north. How far are you from your starting point and what is the compass direction of a line connecting your starting point to your final position? Use a graphical method.

## Solution

Draw a schematic of the path.


Notice that it forms two sides of a right triangle, and the distance between the start and finish points is the length of the hypotenuse.

18.0 m

The Pythagorean theorem relates the sides of a right triangle.

$$
\begin{aligned}
h^{2} & =(18.0 \mathrm{~m})^{2}+(25.0 \mathrm{~m})^{2} \\
h & =\sqrt{18.0^{2}+25.0^{2}} \mathrm{~m} \\
& \approx 30.8 \mathrm{~m}
\end{aligned}
$$

This is how far you are from the starting point.

To find the direction of the line going from start to finish, calculate the angle $\theta$ it makes with the horizontal.

18.0 m

This is a right triangle, so the trigonometric functions apply here. The one which relates the opposite and adjacent sides is the tangent function.

$$
\tan \theta=\frac{\text { opposite }}{\text { adjacent }}=\frac{25.0 \mathrm{~m}}{18.0 \mathrm{~m}} \quad \rightarrow \quad \theta=\tan ^{-1}\left(\frac{25}{18}\right) \approx 54.2^{\circ}
$$

Therefore, the compass direction of the line connecting your starting and finishing points is $54.2^{\circ}$ north of west.

